

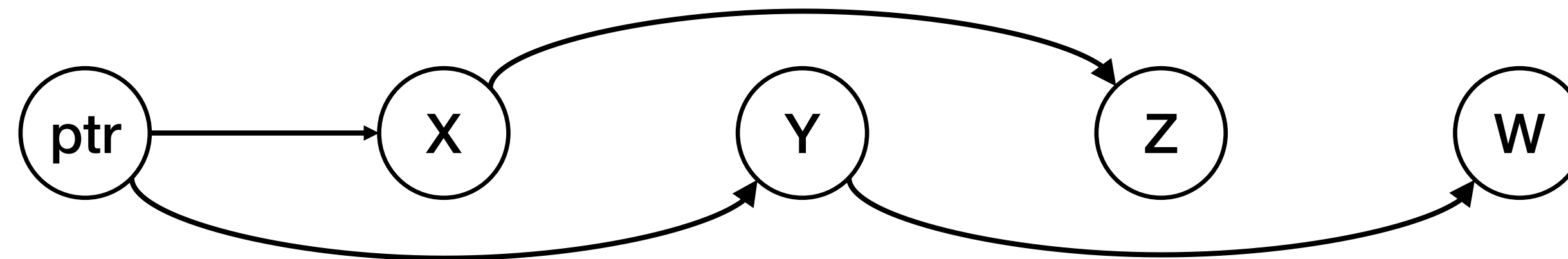
# Flow-Sensitive Pointer Analysis

# flow-sensitive analysis

- Basic data-flow analysis
- Track points-to graph at each point in the program
  - Graphs ordered according to subset inclusion on *edges* of the graph
- All that's left: what are the **transfer functions**?

# notation: points-to sets

- Can think of a points-to graph as a set of **points-to sets**
  - $pt(x)$  = the set of nodes that  $x$  points to = the targets of edges that have  $x$  as a source



- $pt(ptr) = \{x, y\}$
- $pt(x) = \{z\}$

# notation

- Suppose  $S$  and  $S'$  are set-valued variables:  $S = \{x, y\}$  and  $S' = \{x, z\}$
- $S' \leftarrow S$  **strong update**
  - $S'$  has a new value of whatever is in  $S$
  - $S' = \{x, y\}$
- $S' \cup \leftarrow S$  **weak update**
  - Add whatever is in  $S$  to  $S'$
  - $S' = \{x, y, z\}$

# dataflow equations

- Forward analysis (points-to information is about what has already happened)
- Use  $\sqcup$  at merges (points-to information is *may* information)
- Transfer functions:  $G$  is graph before statement,  $G'$  is graph after

address of  
 $x = \& y$

copy  
 $x = y$

load  
 $x = * y$

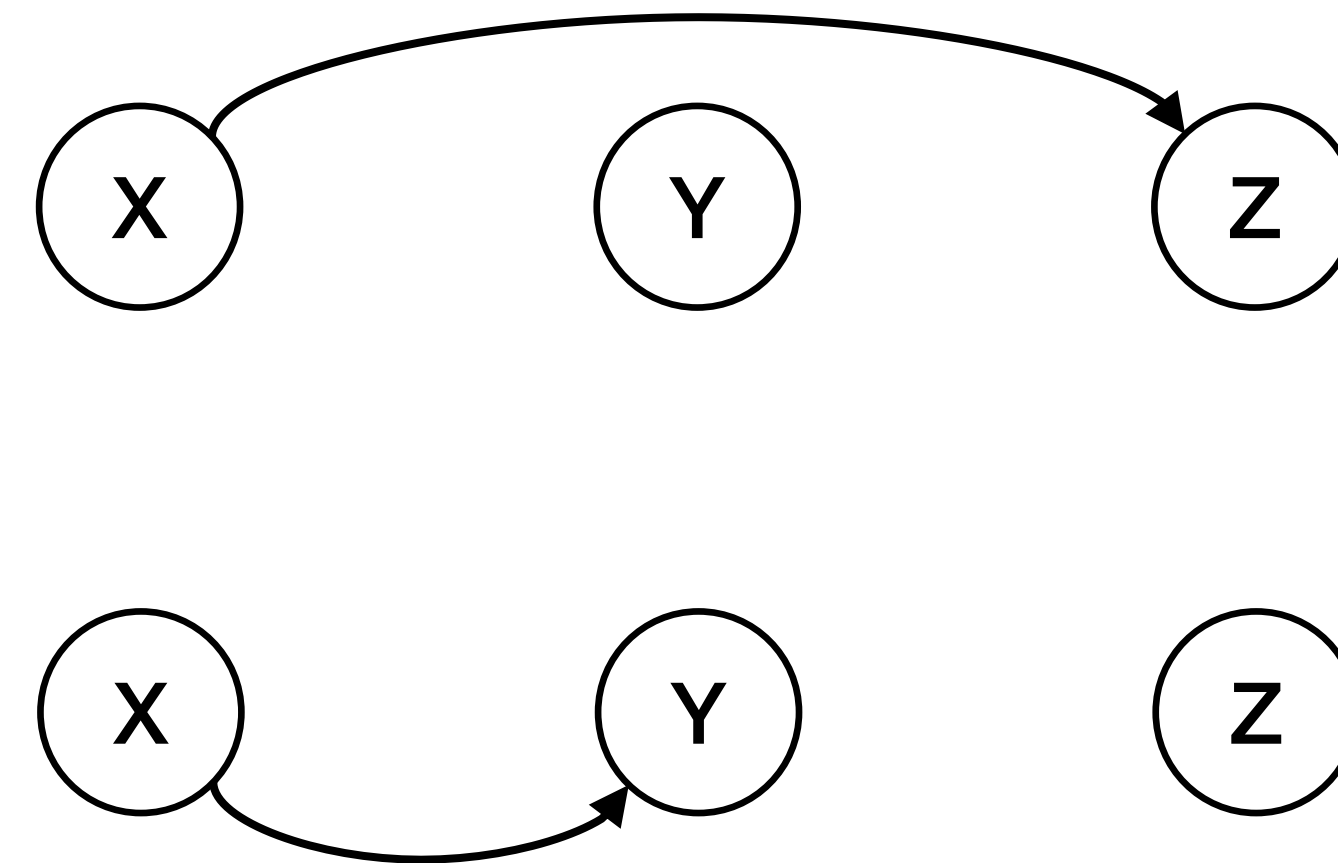
store  
 $* x = y$

# dataflow equations

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$G' = G$  with  $pt(x) \leftarrow \{y\}$

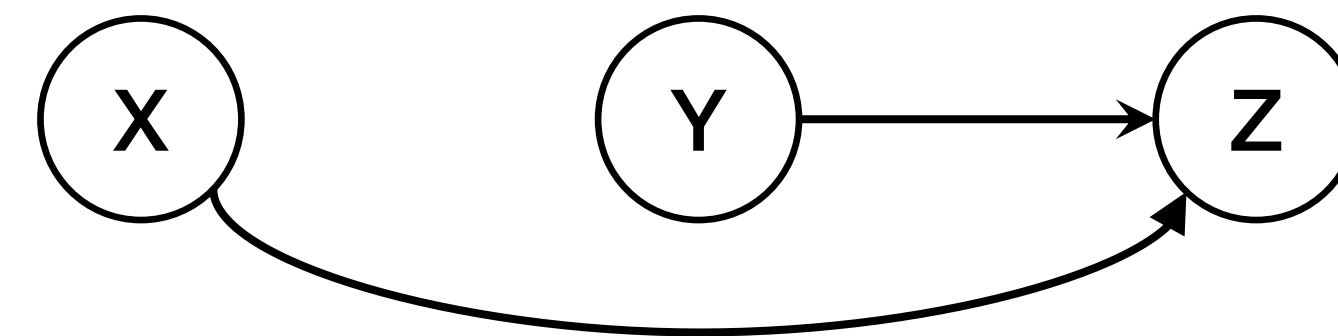
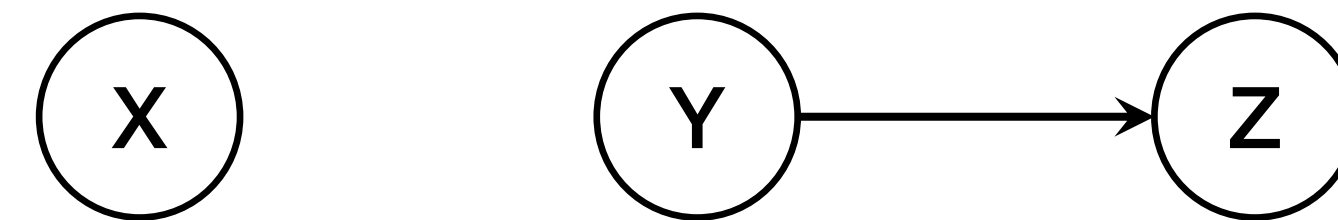


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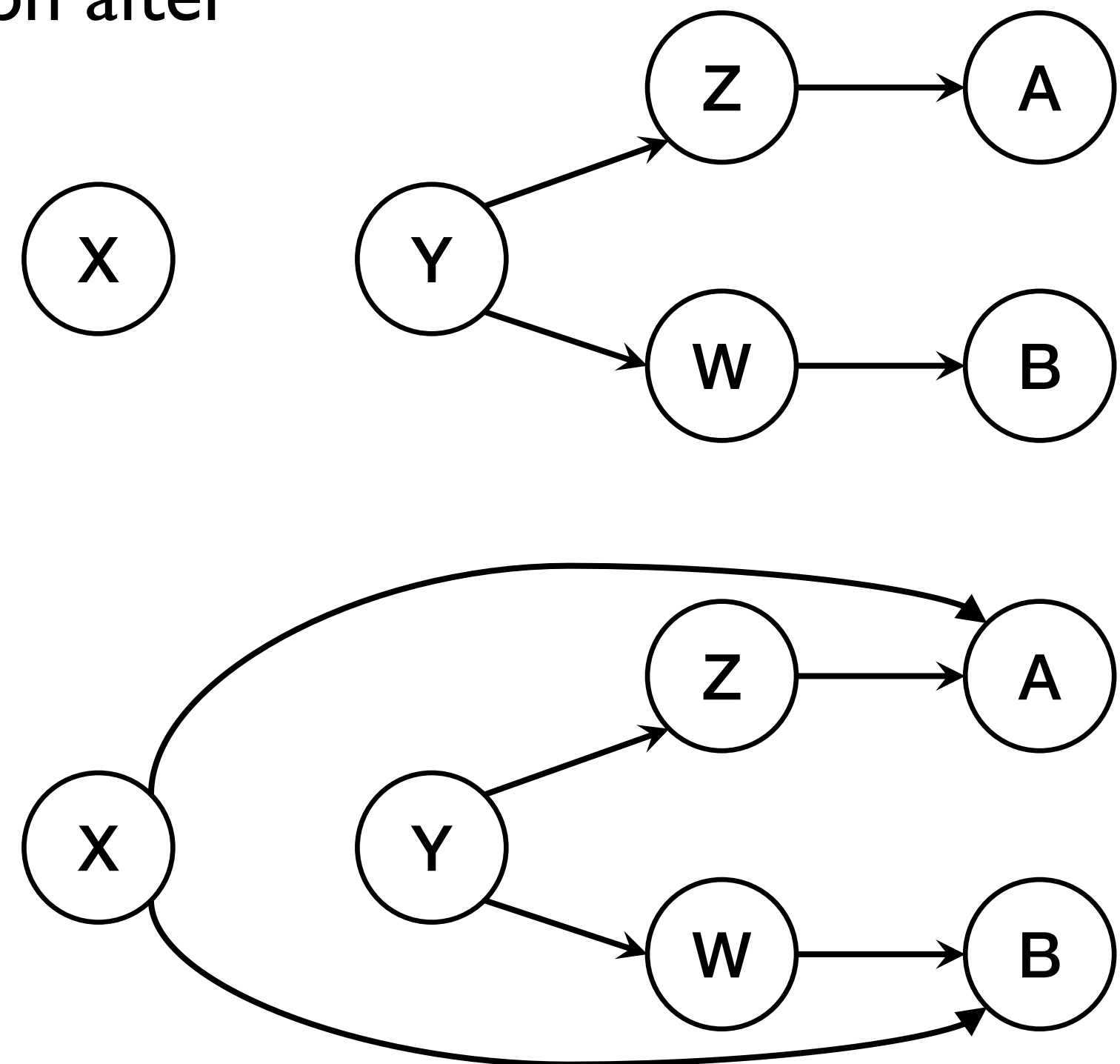


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load  
 $x = *y$

$G' = G$  with  $pt(x) \leftarrow \cup_{a \in pt(y)} pt(a)$



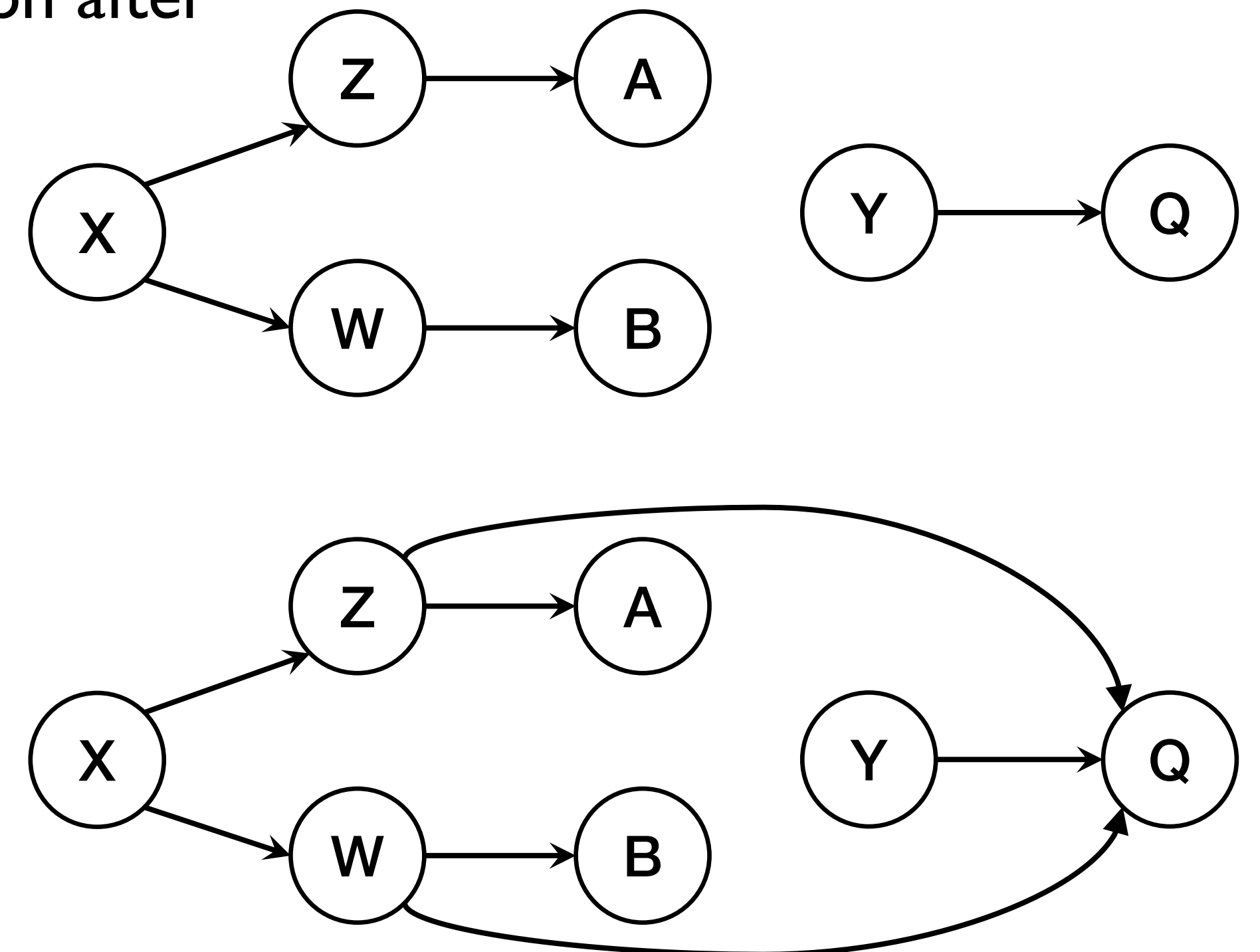


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$G' = G$  with  $\forall a \in pt(x). pt(a) \cup \leftarrow pt(y)$



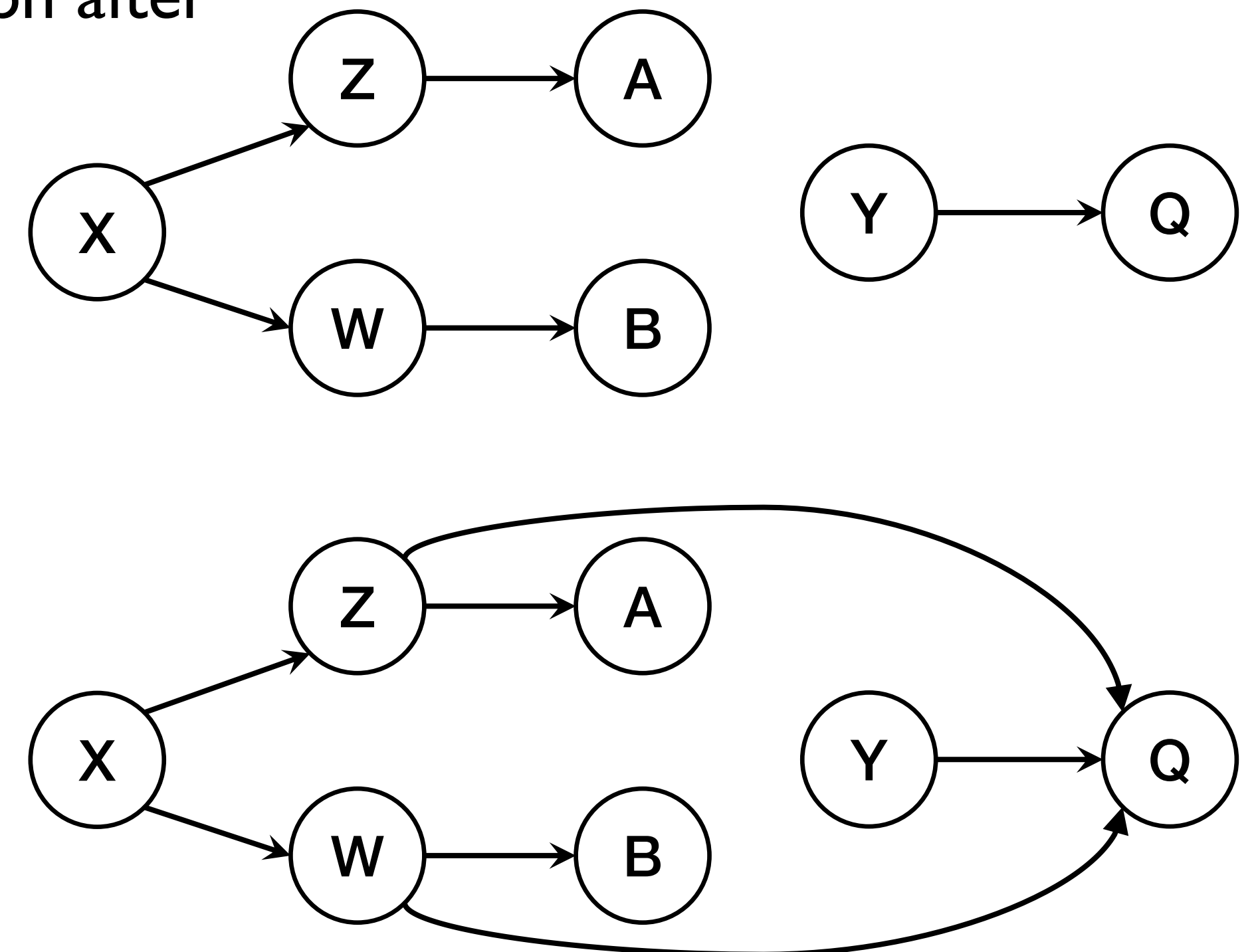
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$$G' = G \text{ with } \forall a \in pt(x). pt(a) \cup \leftarrow pt(y)$$

Weak update! why?



# weak vs. strong updates

- Strong update
  - At an assignment, you know what variables are being written to
  - Can *remove* points-to information coming in to the statement
- Weak update
  - $*x = \dots$  means “whatever  $x$  *points to* should be updated”
  - At runtime, only one variable is written to, but at analysis time, we don’t know which one
  - Each variable *may* be written to, but we cannot safely remove any information

# loads and stores as paths

- One way to keep this straight is to think of loads and stores as multiple paths through the program, one path per thing the pointer points to

load  
`x = *y`

```
//pts(y) = {a, b}  
if (...)  
    x = a  
else  
    x = b
```

store  
`*x = y`

```
//pts(x) = {a, b}  
if (...)  
    a = y  
else  
    b = y
```

**next: flow-insensitive pointer analysis**